Abstract—Sentiment classification is very domain-specific and
good domain adaptation methods, when the training and testing
data are drawn from different domains, are sorely needed. In this
paper, we address a new approach to domain adaptation for
sentiment classification in which classifiers are adapted for a
specific domain with training data from multiple source domains.
We call this new approach ‘multi-domain adaptation’ and present
a multiple classifier system (MCS) framework to describe and
understand it. Under this framework, we propose a new combining
method, called Multi-label Consensus Training (MCT), to combine
the base classifiers for selecting ‘automatically-labeled’ samples
from unlabeled data in the target domain. The experimental
results for sentiment classification show that multi-domain
adaptation using this method improves adaptation performance.

Index Terms—sentiment classification; domain adaptation;
multiple classifier combining.

I. INTRODUCTION

Sentiment classification is the task of classifying documents
according to their opinion, or sentiment, regarding a given
subject matter. Many studies have focused on this task [1]. Most
previous studies, however, are based on the assumption that the
training data is representative of the testing data. This
assumption is routinely incorrect when the application domain
changes. Here, ‘domain adaptation’ is proposed. This usually
involves teaching a classifier using both plentiful labeled data
from the source domain and unlabeled data from the target
domain. Blitzer et al. [2] discuss precisely this problem where a
structural correspondence learning (SCL) algorithm is applied
to sentiment classification and shown to be successful when an
appropriate domain is chosen to match the target domain.

Sentiment classification is a very domain-specific problem
[3], and adaptation algorithms successful in one domain to
another are extremely difficult. Using learning data from only a
single domain to teach adaptation for other domains is not
feasible because adaptation fails totally when the data
distribution in the target domain is very different from that in
the source domain [2]. We, therefore, suggest improving
adaptation results by using multiple domains to source learning
data. In the rest of this paper this new approach of domain
adaptation is called multi-domain adaptation, while adaptation
from one domain to another is referred to as one-to-one
adaptation. For multi-domain adaptation, we can firstly apply an
adaptability measurement to select the domain with the best
adaptability and then use one-to-one adaptation algorithms.
Consider, for example, labeled product reviews from three
different domains: books, DVDs, and electronics, and we want
to teach a classifier with documents discussing kitchens. Since
the electronics domain shows the best computed adaptability [2],
labeled data from the electronics domain is selected to train a
classifier. One major drawback of this method for multi-domain
adaptation is that it drops the labeled data from the other
domains that may contain helpful information. We believe there
are superior methods that can make full use of all the available
labeled data.

In this paper, we present a multiple classifier system (MCS)
framework to describe and understand the approach of
multi-domain adaptation. Constructing an MCS generally
consists of two steps: training a number of component
classifiers then using combination rules to combine them. In the
first step, classifiers can be trained in different ways including
using different learning algorithms, training data, and feature
sets. These component classifiers are usually called the base
classifiers. In multi-domain adaptation, they can be naturally
obtained using labeled data from different domains. There are
various rules presented in the MCS literature to combine the
base classifiers in the second step. The architecture of the MCS
framework for multi-domain adaptation is shown in Figure 1.
II. OUR FRAMEWORK

In a standard classification problem, a classifier is the predicting function that maps an input vector to the corresponding output. Usually, the classifier is trained using training samples and then used to predict other label-unknown samples. In domain adaptation, the training samples and the label-unknown samples do not come from the same domain. In other words, the testing (target) data and the training (source) data are drawn from different statistical distributions. As far as multi-domain adaptation is concerned, the training samples themselves come from different domains while the testing samples are from another domain which is different from all the multiple source domains.

Multi-domain adaptation can be simplified to one-to-one adaptation in two straightforward ways. The first is to simply mix the training samples from all domains and then to train a classifier with the mixed data. This method has been pursued by Aue and Gamon [3] as a baseline, and is named all-data. It is outside the scope of our MCS framework since it only uses one classifier; and belongs to a framework we call add-all as shown in Figure 2. The second way is to use the samples from the domain with the best adaptability where the adaptability is evaluated by some measurement (e.g., to compute A-distance between two domains using unlabeled data) [2].

We approach this problem from a different perspective. In multi-domain adaptation, multiple base classifiers can be naturally obtained using labeled data from different domains. Given these multiple classifiers, the problem can be treated as a typical MCS problem. Note that the second method mentioned above can be seen as an instance of the MCS framework where the classifier combination rule is select-best. There are some notable advantages to treating this problem as an MCS problem:

1. The idea that one can benefit from combining multiple classifiers has been widely proposed in various research areas including: pattern recognition, machine learning and natural language processing. In particular, combining classifiers trained naturally from different sources is extremely effective for the overall performance improvement.

2. MCS, as an important research field, has been studied intensively over the last decade [4]. Many problems in this field that could help us better understand multi-domain adaptation have been addressed and solved. For example, an important issue in MCS is the classifier selection problem that states that good classifiers should be selected for combination rather than all [5]. The same issue can be found in multi-domain adaptation in terms of whether we need to select good source domains for adaptation rather than using all.

3. MCS possesses a great many well-designed combination rules. Once a suitable MCS mode is built, the corresponding rules can be directly borrowed or slightly modified to deal with the current problem.

Generally speaking, domain adaptation can be divided into two main categories [6]. In the first, called fully supervised, a few labeled samples are used in the learning process. In the second, called semi-supervised, only unlabeled samples are available for the learning process. In multi-domain adaptation, different categories demand different base classifiers and methods of combination. In accordance with the MCS framework, let us give our methods for multi-domain adaptation in two steps: training base classifiers and combining base classifiers; these are described in Sections 3 and 4 respectively.

III. TRAINING BASE CLASSIFIERS

The first step in constructing an MCS is to train multiple base classifiers. In the fully supervised case, each base classifier can be directly trained with the labeled data from both each source domain and the target domain. In the semi-supervised case, each base classifier is trained using labeled data from each source domain.
domain and unlabeled data from the target domain simultaneously. To do this, a structural correspondence learning (SCL) algorithm is used to train multiple one-to-one adaptation classifiers. The SCL algorithm represents the state-of-the-art in domain adaptation and has been shown to be very effective in sentiment classification [2]. We provide a basic description of this algorithm below. For a detailed description, please see Blitzer et al. [7].

The input data for SCL is labeled data from the source domain and unlabeled data from the target domain or both domains. Generating a classifier more suitable for classification of data in the target domain consists of three main steps. First, pivot features that occur frequently in both domains are selected. Second, correlations are modeled between the pivot features and all other features by training with linear classifiers to classify occurrences of each pivot in all unlabeled data. Finally, with the help of the correlations, the classifier is trained on the labeled source domain data that also provides the influence of the unseen features in the training data.

In sentiment classification, pivot features with high mutual information (MI) are especially helpful for the adaptation [2]. Therefore, we select the pivot features from the top-10% MI features in our experiments.

IV. CLASSIFIER COMBINING METHODS

A. Fully-supervised methods

In the supervised case, various trained combination rules, such as the weighted sum rule, Dempster-Shafer and the weighted voting rule can be "borrowed" [8] [9]. Among these trained methods, a class of methods called meta-learning has been shown to be very effective. The key idea behind this class is to train a meta-classifier with input attributes that are the output of the base classifiers [10].

Aue and Gamon [3] have considered precisely this case for multi-domain adaptation and use the meta-learning combination rule. Their experimental results using small labeled samples in the target domain show significant improvement over the all-data method in some, but not all, domains. Since the number of labeled samples can not be large (otherwise, the adaptation is not necessary), meta-learning becomes difficult. As a result, making use of a large amount of unlabeled samples in the target domain seems to be very promising as acquiring unlabeled samples is much easier.

B. Semi-supervised methods

Unlike the supervised case, there have been very few methods proposed for semi-supervised MCS [11]. Didaci and Rolli [12] propose two general methods for semi-supervised MCS using co-training and self-training, called the extended co-training algorithm and the ensemble-driven self-training algorithm. With the help of their work, we propose the ensemble-driven self-training algorithm for multi-domain adaptation shown in Figure 3. The basic idea of this algorithm is to label some of the unlabeled data with high classification confidence with an MCS, and then put the 'automatically-labeled' data into the training data of each source domain.

### Ensemble-driven Self-training for Multi-domain Adaptation

**Input:**
- (a) $m$ sets $L_k$ ($k = 1, \ldots, m$) of labeled training samples from $m$ different source domains
- (b) a set $U$ of unlabeled samples from the target domain

**Algorithm:**

1. Create a set $U'$ of samples by choosing $n$ samples at random from $U$
2. Loop for $N$ iterations:
   - (1) Build $m$ classifiers $c_k$ using both $L_k$ and $U'$ with the one-to-one adaptation algorithm
   - (2) Create a MCS using $\{ c_k \}$
   - (3) Run MCS on $U'$
   - (4) For each class $j$
     - Select the $n_j$ samples assigned to the class $j$ by the MCS with the highest confidence
   - (5) Add these $m \times \sum n_j$ self-labeled samples to each $L_k$
   - (6) Randomly choose $m \times \sum n_j$ samples from $U$ to replenish $U'$

**Output:**

New base classifiers $\{ c_k \}$ trained on the new $L_k$ and $U$ with the one-to-one adaptation algorithm

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Figure 3: The ensemble-driven self-training algorithm applied to multi-domain adaptation

This semi-supervised algorithm is a general algorithm. Two operations in the algorithm need to be specified for any given task: the one-to-one adaptation algorithm and the combining rule to construct the MCS. For sentiment classification, the one-to-one adaptation algorithm applied is the SCL algorithm introduced above. With respect to the combination rule here, it must satisfy two basic requirements: (1) it can select unlabeled samples from the target domain; (2) these selected samples are classified with a very high accuracy. Accordingly, we define two functions whose input is one sample $x$ and corresponding output represents whether an event related to $x$ happens:
$E_1(x) = \begin{cases} 1 & \text{x is selected by MCS} \\ 0 & \text{x is not selected by MCS} \end{cases}$

and

$E_2(x) = \begin{cases} 1 & \text{The selected x is correctly classified} \\ 0 & \text{The selected x is not correctly classified} \end{cases}$

According to the definition, we have

$P(E_1(x) = 1) = P(l_{\text{mcs}}(x) = \text{real}(x) | E_1(x) = 1) \quad (1)$

where $l_{\text{mcs}}$ is the class label of the sample assigned by the MCS and the function $\text{real}(x)$ returns the real class label. To obtain some high-precision ‘automatically-labeled’ samples from the target domain, we should guarantee a high probability of $P(E_1(x) = 1)$ and also not a too low probability of $P(E_1(x) = 0)$.

From previous studies, we find that the best base classifier often achieves much higher accuracy than other base classifiers and even the MCS. One example is a supervised case that combines all the base classifiers using 50 training samples from the target domain. All the adaptation results using meta-learning are worse than using the select-best rule (comparing Table 1 with Table 5 in Aue and Gamon [3]). Another example is a semi-supervised case in which it was reported that, for any fixed amount of labeled data, it is always better to draw from the nearest domain as a source than using some combination of all available domains [2]. Given these findings, our combination rule needs to select samples with a higher precision than the best base classifier when using MCS. Thus we select samples whose labels assigned by the base classifiers are the same. That is to say, an sample is selected and assigned to class $j$ when the class labels assigned by all the base classifiers are consistent, i.e.,

$E_1(x) = 1$ and $l_{\text{mcs}} = j$ if and only if $l_1(x) = \ldots = l_n(x) = l_{\text{mcs}}(x) = j \quad (2)$

Where $l_i(x)$ is the class label assigned by the $i$-th base classifier. For simplicity, we call this rule Multi-label consensus and the ensemble-driven self-training algorithm using this combining rule Multi-label Consensus Training (MCT). Note that the outputs of this algorithm are still multiple one-to-one adaptation classifiers. These new classifiers are called MCT classifiers.

The rule of Multi-label consensus has the advantage that it guarantees that the MCS selects samples with a higher accuracy than the best classifier. We prove this advantage below.

Each base classifier $c_i$ achieves accuracy $A_i$, which can also be seen as the estimation of the probability $P(l_i(x) = \text{real}(x))$ that a test sample is correctly classified by this classifier. For simplicity, it is briefly denoted as $P_i$. We assume:

(I) $P_i > 1 - P_i$, i.e., $P_i > 0.5$, which means each base classifier achieves accuracy higher than a random classification of a binary classification problem. This assumption is easily satisfied in real applications, and;

(II) The probabilities of each $P_i$ are independent of each other. Although this assumption is hard to make hold in real applications, it can be approximately satisfied in multi-domain adaptation where the base classifiers are trained using different features and also different data sets.

Given the condition (2) and the assumption (I), we find

$P(l_{\text{mcs}}(x) = \text{real}(x)) = P_1 \cdot P_2 \cdots P_n \quad (3)$

According to the definition of $E_1(x)$ and the condition (2), we have

$P(E_1(x) = 1) = P(l_1(x) = \ldots = l_n(x) = \text{real}(x)) + P(l_1(x) = \ldots = l_n(x) \neq \text{real}(x)) \quad (4)$

Since sentiment classification we care about here is a binary classification problem, we have

$P(l_1(x) = \ldots = l_n(x) \neq \text{real}(x)) = P(l_1(x) \neq \text{real}(x), \ldots, l_n(x) \neq \text{real}(x)) \quad (5)$

Consider the conclusion that if two events are independent from each other then their complement events are also independent, we have

$P(l_1(x) = \ldots = l_n(x) \neq \text{real}(x)) = (1 - P_1)(1 - P_2) \cdots (1 - P_n) \quad (6)$

According to (3), (4), (6), and (1), we get

$P(E_2(x) = 1) = \frac{P_1 \cdot P_2 \cdots P_n}{P_1 \cdot P_2 \cdots P_n + (1 - P_1)(1 - P_2) \cdots (1 - P_n)} \quad (7)$

To guarantee that $P(E_2(x) = 1)$ is larger than $P_{\text{best}}$, the probability that one test sample is correctly classified by the best base classifier, the following formula must be satisfied:

$P(E_2(x) = 1) / P_{\text{best}} > 1 \quad (8)$

which can be rewritten as:

$\frac{P_1 \cdots P_{\text{best}-1}}{P_1 \cdots P_{\text{best}-1} + (1 - P_1) \cdots (1 - P_{\text{best}-1})} > 1 \quad (9)$

The above condition is equivalent to:

$P_1 \cdots P_{\text{best}-1} \cdot (1 - P_{\text{best}}) \cdots (1 - P_n) > (1 - P_1) \cdots (1 - P_{\text{best}})(1 - P_n) \quad (10)$

This condition is satisfied using the assumption (I). Therefore, given the two assumptions, the Multi-consensus rule guarantees that MCS selects samples with a higher accuracy than the best classifier. It is worth pointing out that this rule is designed for multi-domain sentiment classification when the number of
source domains is small. When the number increases, this selecting strategy is too strict to select enough ‘automatically-labeled’ data as \( P(E_{u}(x) = 1) \) becomes very small. Thus, the selecting strategy needs to be modified for large numbers of source domains. For example, we can demand that a fixed number of output labels are consistent and also includes the label from the best base classifier.

Let us also consider the iteration number \( N \) in MCT. Since our base classifiers are trained using different data sets, the diversity among these classifiers becomes smaller when more ‘automatically-labeled’ samples are added. As a result, the ‘automatically-labeled’ data gradually takes the dominant place in the base classifiers. As these are not true labeled data, classification errors accumulate quickly as the iteration time grows. Moreover, using the same ‘automatically-labeled’ samples in each new base classifier makes the assumption (II) for the Multi-label consensus rule harder to satisfy. Therefore, the selecting process is performed only once across all unlabeled data \( U \).

Note that there is another semi-supervised method, the extended co-training algorithm, in Didaci and Roli [12] which can also be applied to multi-adaptation. It shares the same basic idea as the ensemble-driven self-training algorithm, except in selecting the samples using each base classifier rather than MCS. This algorithm is not suitable, however, for sentiment classification because sentiment classification is very domain-specific and classifiers trained in one domain may perform very badly on the target domain even given the adaptation process. For example, to classify reviews of books, an adaptation classifier using labeled reviews of kitchen appliances performs much worse than one using DVDs. Clearly, adding the ‘automatically-labeled’ samples from these bad classifiers only adds noisy information.

V. EXPERIMENTS

As the supervised case has been experimentally studied using meta-learning in Aue and Gamon [3], we do not consider this case in our experiments. Our experimental studies concentrate on multi-domain adaptation of sentiment classification in the semi-supervised case.

Data Set¹: our experiments are carried out on a data set of product reviews from four domains: books, DVDs, electronics and kitchen appliances, B, D, E and K, for short, in the tables and figures. This data was assembled by Blitzer et al. [2] and used to evaluate the SCL algorithm in sentiment classification. Each domain has 1,000 positive and 1,000 negative samples. Besides the labeled data, large amounts of unlabeled samples are available in this data set. The unlabeled samples are disregarded here. Instead, the labeled samples in one domain are used as unlabeled samples when this domain is the target domain in the adaptation process.

Classification Algorithm: Following Blitzer et al. [2], we use linear predictors on unigram and bi-gram features, trained to minimize Huber loss with stochastic gradient descent [13]. To implement adaptation for one-to-one domains in the semi-supervised case, we apply the SCL algorithm which has been introduced in Section 3.

Experiment Implement: For each domain, we first split the labeled data into 5 folds. Then, we select 4 folds for training and use the remaining one fold for testing. As a result, 5 different distributions are obtained for each domain. Similarly, we get 5 different distributions for the whole data set by selecting the distribution from each domain sequentially: selecting the first distribution of each domain, then the second, the third and so on. All the experiments below are run on these 5 different distributions of the complete data set and the reported result is the mean value of the accuracies of the 5 runs.

Baseline and Gold Standard: The baseline is a linear classifier trained without adaptation, while the gold standard is an in-domain classifier trained on the same domain as it is tested. Classification accuracies are reported in Table 1 where the first column represents the source domains and the values in the diagonal are the results of the gold standard.

<table>
<thead>
<tr>
<th>Source Domain</th>
<th>B</th>
<th>D</th>
<th>E</th>
<th>K</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>0.87</td>
<td>0.765</td>
<td>0.704</td>
<td>0.733</td>
</tr>
<tr>
<td>D</td>
<td>0.747</td>
<td>0.837</td>
<td>0.696</td>
<td>0.713</td>
</tr>
<tr>
<td>E</td>
<td>0.690</td>
<td>0.683</td>
<td>0.842</td>
<td>0.795</td>
</tr>
<tr>
<td>K</td>
<td>0.672</td>
<td>0.686</td>
<td>0.787</td>
<td>0.840</td>
</tr>
</tbody>
</table>

Table 1: Mean accuracy results using the baseline and gold standard.

First, let us consider the iteration number \( N \) in MCT. The quality of the adaptation decreases slightly as the iteration number \( N \) increases. The reason for this decrease was proposed in the last section. Due to a limited space, we only give the results when \( N=1 \).

¹ The data set is available at [http://www.seas.upenn.edu/~mdredze/datasets/sentiment/](http://www.seas.upenn.edu/~mdredze/datasets/sentiment/)
Figure 4 presents the results for all pairs of domain adaptation. The main difference between base and MCT classifiers is that MCT classifiers use ‘automatically-labeled’ samples as additional training data in the target domain while base classifiers do not. From the results, we can see that these ‘automatically-labeled’ samples play a very important role in the adaptation process, especially when the source domain is very different from the target domain. Even when the domains are similar (and the best performance is achieved), the MCT classifier consistently shows superior performance to the base classifiers. More specifically, the best MCT classifiers on the target domains B, D, E, and K reduce the error by 12.6%, 5.4%, 3.1%, and 9.3% using source domains D, B, K, and E respectively. Note that the performance from domain D to domain B shows the most impressive error reduction of 12.6%. We think this is mainly due to differences in the performances of the base classifiers not being too large, e.g., the performance of the best base classifier is 0.747 which is only 0.046 better than 0.701 for the second best classifier. The distances are much larger when the target domains are D, E, and K, which are 0.07, 0.08, and 0.065 respectively.

These results are encouraging because they suggest a better adaptation approach: when training data from multiple domains is available, combining them produces better results than selecting only the best, especially when the multiple domains show similar adaptabilities.

Table 2 shows the two probabilities of $P(E_1(x) = 1)$ and $P(E_2(x) = 1)$ which are estimated as

$P(E_1(x) = 1) = \frac{\text{the number of selected unlabeled samples}}{\text{the number of all unlabeled samples}}$

$P(E_2(x) = 1) = \frac{\text{the number of correctly classified samples}}{\text{the number of selected unlabeled samples}}$

From the results, we observe that MCS achieves a much higher precision than any single base classifier, which can explain why our method does work.

<table>
<thead>
<tr>
<th>Probability</th>
<th>B</th>
<th>D</th>
<th>E</th>
<th>K</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P(E_1(x) = 1)$</td>
<td>0.581</td>
<td>0.595</td>
<td>0.600</td>
<td>0.597</td>
</tr>
<tr>
<td>$P(E_2(x) = 1)$</td>
<td>0.872</td>
<td>0.864</td>
<td>0.876</td>
<td>0.908</td>
</tr>
</tbody>
</table>

Table 2: The two probabilities estimated through testing on unlabeled samples in the target domains: B, D, E, and K by the multi-consensus MCS respectively.

Besides our MCS framework, there exist other models that can be used to describe the task of multi-domain adaptation. One straightforward model is to mix labeled data from all available domains, (mentioned in Section 2 as add-all). We provide a comparison result in Figure 5 where add-all denotes an SCL classifier trained using both labeled samples from all source domains and unlabeled samples from the target domain. The result demonstrates that although this model can sometimes
outperform selecting the best base classifiers, it is consistently worse than selecting the best MCT classifier.

VI. RELATED WORK

To the best of our knowledge, there have been very few previous studies that directly investigate the problem of multi-domain adaptation. There are two related studies that have discussed solutions for this task for the fully supervised case. The first is reported by Aue and Gamon [3] who apply meta-learning to combine classifiers as they are applied here. The second, from Daume III [6], is the feature augmentation method which is proposed for one-to-one domain adaptation and is easily extended to the multi-domain case. This method can be seen as a special case of the all-all method that mixes all data with augmented input features. However, neither of these two methods is suitable for the semi-supervised case as discussed in this paper since they cannot deal with unlabeled data.

VII. CONCLUSION AND FUTURE WORK

In summary, the contribution of this paper is twofold. First, we provide an MCS framework to describe multi-domain adaptation. Under this framework, we seek methods for this problem in two cases: ‘fully supervised’ and ‘semi-supervised’. Second, we propose an MCS driven self-training combination method called MCT for the semi-supervised case and theoretically prove that this method selects ‘automatically labeled’ samples with a higher accuracy than using the best base classifier. Experimental results demonstrate that ‘automatically labeled’ samples from MCT can greatly improve adaptation. This good performance confirms that when data from multiple source domains is available, its combination is an effective way to improve adaptation performance.

It is worth pointing out that although this work is motivated by and evaluated for adaptation of sentiment classification, the general framework is suitable for other classification problems. It will be interesting to investigate this new task for other NLP problems, e.g., parsing, name entity recognition and so on; this will be the subject of future work.

REFERENCES